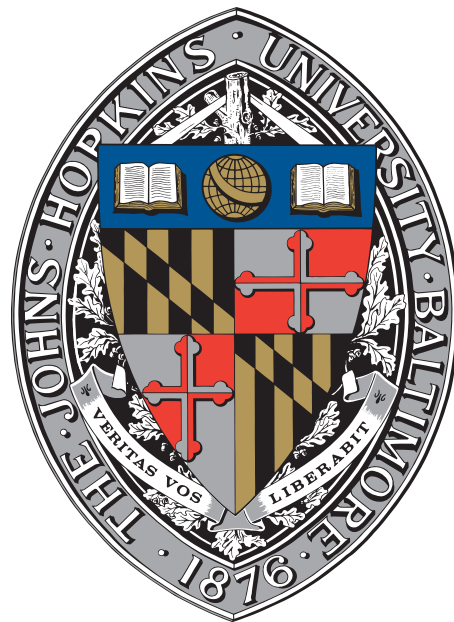


Status of Higgs CP Studies

Andrei Gritsan

Johns Hopkins University



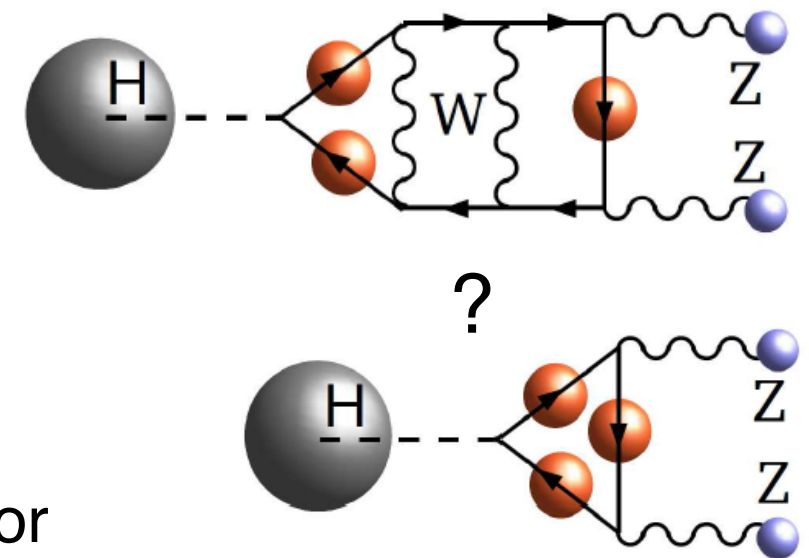
September 1, 2021

Snowmass Energy Frontier Workshop, EF01/02 Session

CP-violating H(125) Couplings

- CP-violating H(125) couplings

- tiny in the SM, excellent null-test
- well-defined stand-alone reference measurement
- potential baryogenesis connected to the Higgs sector
- input to the global EFT fits, which currently focus on CP-even Operators
- $pp, e^+e^-, \gamma\gamma, \mu^+\mu^- (\sqrt{s})$ have their unique features in CP of H(125)
- complementarity to the EDM measurements and Flavor Physics



- Identify key reference measurements to compare facilities

- focus on direct H production (including off-shell)
- connect to indirect (virtual, low-energy) probes

EFT Approach to CP

- Tradeoff between **complexity/reach** and **simplicity/scope**

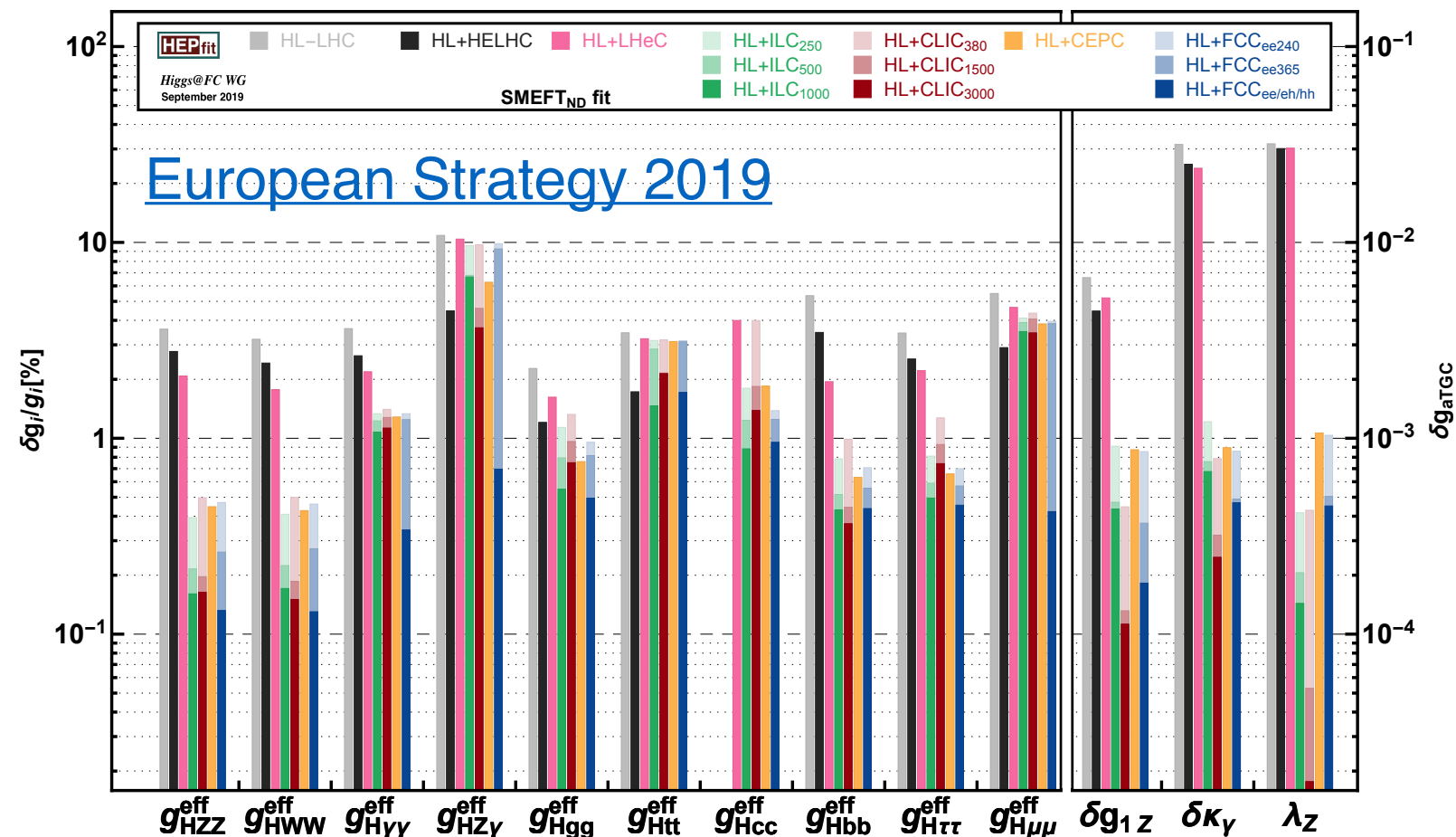
— what is better to illustrate certain point: **implications for colliders?**

e.g. effective couplings were chosen for European Strategy (CP-even):

$$g_{HX}^{\text{eff } 2} \equiv \frac{\Gamma_{H \rightarrow X}}{\Gamma_{H \rightarrow X}^{\text{SM}}} \rightarrow$$

- look for structure
if we include CPV:

$$f_{\text{CP}}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$



([Snowmass-2013](#))

$$\text{SMEFT}_{\text{ND}} \equiv \left\{ \delta m, c_{gg}, \delta c_z, c_{\gamma\gamma}, c_{z\gamma}, c_{zz}, c_{z\Box}, \delta y_t, \delta y_c, \delta y_b, \delta y_\tau, \delta y_\mu, \lambda_z \right\} \\ + \left\{ (\delta g_L^{Zu})_{q_i}, (\delta g_L^{Zd})_{q_i}, (\delta g_L^{Zv})_\ell, (\delta g_L^{Ze})_\ell, (\delta g_R^{Zu})_{q_i}, (\delta g_R^{Zd})_{q_i}, (\delta g_R^{Ze})_\ell \right\}_{q_1=q_2 \neq q_3, \ell=e,\mu,\tau}$$

Higgs CP from Snowmass-2013

- Higgs Working Group Report of the **Snowmass-2013** Community Planning Study

Chapter 1.4 devoted to spin and CP: [arXiv:1310.8361](https://arxiv.org/abs/1310.8361)

— $pp, e^+e^-, \gamma\gamma, \mu^+\mu^- (\sqrt{s})$ have their unique features in CP of H(125)

Collider	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	$\gamma\gamma$	$\mu^+\mu^-$	target (theory)
E (GeV)	14,000	14,000	250	350	500	1,000	126	126	
\mathcal{L} (fb $^{-1}$)	300	3,000	250	350	500	1,000	250		
spin-2 $_m^+$	$\sim 10\sigma$	$\gg 10\sigma$	$> 10\sigma$	$> 10\sigma$	$> 10\sigma$	$> 10\sigma$	spin=0 established by now		
VVH^\dagger	0.07	0.02	✓	✓	✓	✓	✓	✓	$< 10^{-5}$
VVH^\ddagger	$4 \cdot 10^{-4}$	$1.2 \cdot 10^{-4}$	$7 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	—	—	$< 10^{-5}$
VVH^\diamond	$7 \cdot 10^{-4}$	$1.3 \cdot 10^{-4}$	✓	✓	✓	✓	—	—	$< 10^{-5}$
ggH	0.50	0.16	—	—	—	—	—	—	$< 10^{-2}$
$\gamma\gamma H$	—	—	—	—	—	—	0.06	—	$< 10^{-2}$
$Z\gamma H$	—	✓	—	—	—	—	—	—	$< 10^{-2}$
$\tau\tau H$	✓	✓	0.01	0.01	0.02	0.06	✓	✓	$< 10^{-2}$
ttH	✓	✓	—	—	0.29	0.08	—	—	$< 10^{-2}$
$\mu\mu H$	—	—	—	—	—	—	—	✓	$< 10^{-2}$

† estimated in $H \rightarrow ZZ^*$ decay mode

‡ estimated in $V^* \rightarrow HV$ production mode

$^\diamond$ estimated in $V^*V^* \rightarrow H$ (VBF) production mode

$$f_{\text{CP}}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$

Higgs CP from Snowmass-2013

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— $pp, e^+e^-, \gamma\gamma, \mu^+\mu^- (\sqrt{s})$ have their unique features in CP of H(125)

Collider	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	$\gamma\gamma$	$\mu^+\mu^-$	target (theory)
E (GeV)	14,000	14,000	250	350	500	1,000	126	126	
\mathcal{L} (fb $^{-1}$)	300	3,000	250	350	500	1,000	250		
spin-2 $_m^+$	$\sim 10\sigma$	$\gg 10\sigma$	$> 10\sigma$	$> 10\sigma$	$> 10\sigma$	$> 10\sigma$			$> 5\sigma$
VVH^\dagger	0.07	0.02	✓	✓	✓	✓	✓	✓	$< 10^{-5}$
VVH^\ddagger	$4 \cdot 10^{-4}$	$1.2 \cdot 10^{-4}$	$7 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$	—	—	$< 10^{-5}$
VVH^\diamond	$7 \cdot 10^{-4}$	$1.3 \cdot 10^{-4}$	✓	✓	✓	✓	—	—	$< 10^{-5}$
ggH	0.50	0.16	—	comparison across facilities				—	$< 10^{-2}$
$\gamma\gamma H$	—	—	—	—	—	—	0.06	—	$< 10^{-2}$
$Z\gamma H$	—	✓	—	—	—	—	—	—	$< 10^{-2}$
$\tau\tau H$	✓	✓	0.01	0.01	0.02	0.06	✓	✓	$< 10^{-2}$
ttH	✓	✓	—	—	0.29	0.08	—	—	$< 10^{-2}$
$\mu\mu H$	—	—	—	—	—	—	—	✓	$< 10^{-2}$

targeted couplings

theoretical interest

parameters of interest $f_{\text{CP}}^{\text{HX}} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$

† estimated in $H \rightarrow ZZ^*$ decay mode
 ‡ estimated in $V^* \rightarrow HV$ production mode
 ◇ estimated in $V^*V^* \rightarrow H$ (VBF) production mode

Target for Snowmass-2022

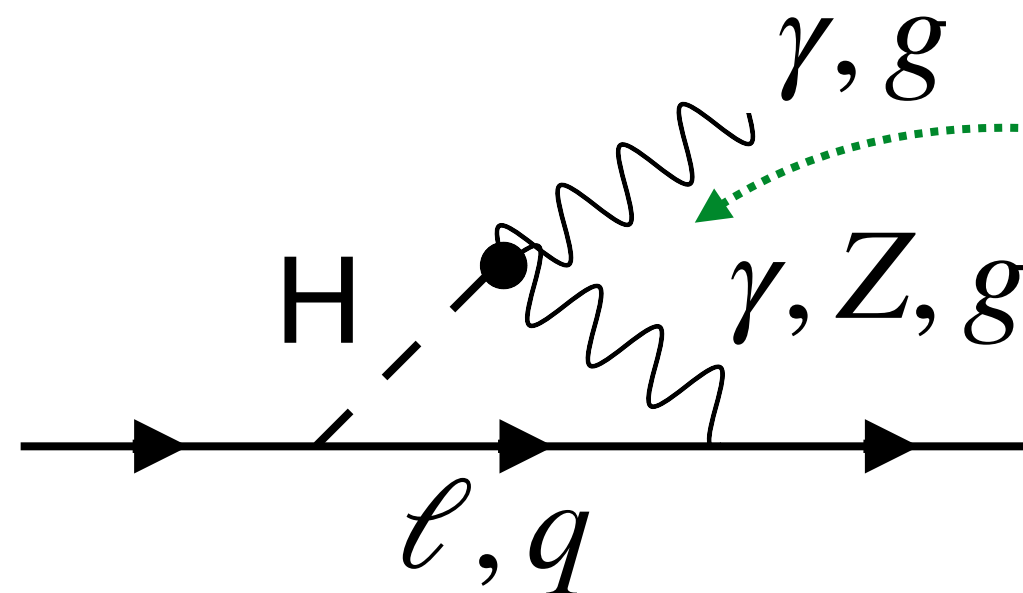
- Revisit Snowmass-2013 studies
 - new realist LHC studies appeared
 - e.g. CP in $H\tau\tau$, $H\tau\tau$, Hgg
 - recent update from Higgs Physics at the HL-LHC and HE-LHC
 - new phenomenological studies performed
 - Effective Field Theory approach gained popularity
 - any new ideas, techniques, studies to be incorporated
- Plan to collect input in a Higgs CP writeup:
 - Gitlab area created: <https://gitlab.cern.ch/snowmass21-ef01/higgs-cp>

“Table-Top,” “Lower-Energy,” Direct H production

- Electric Dipole Moment (EDM) of electron $d_e < 1.1 \times 10^{-29} e \text{ cm}$

$$d_e^{\text{SM}} \sim 10^{-38} e \text{ cm}$$

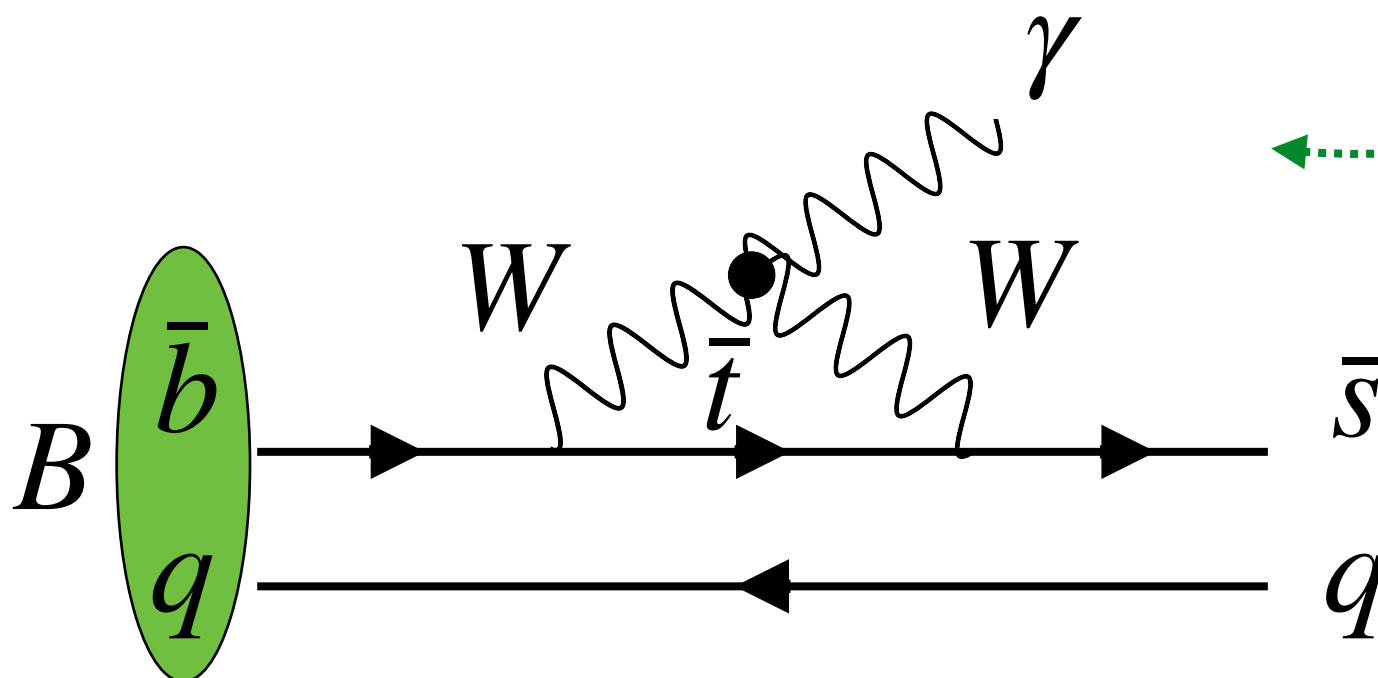
$$d_n < 3.0 \times 10^{-26} e \text{ cm}$$



complementary in EFT

SU(2)xU(1)

- Heavy-Quark meson decays:



Theoretical Models and connection to EDM/B/EW

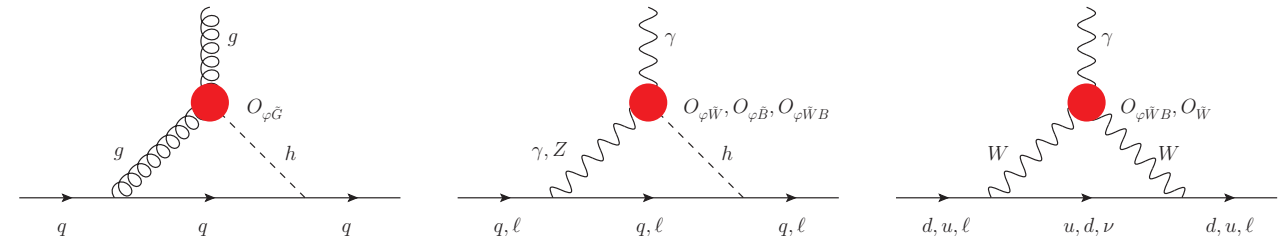
• Representative model analysis

Hff in 2HDM: [arXiv:1304.0773](https://arxiv.org/abs/1304.0773)

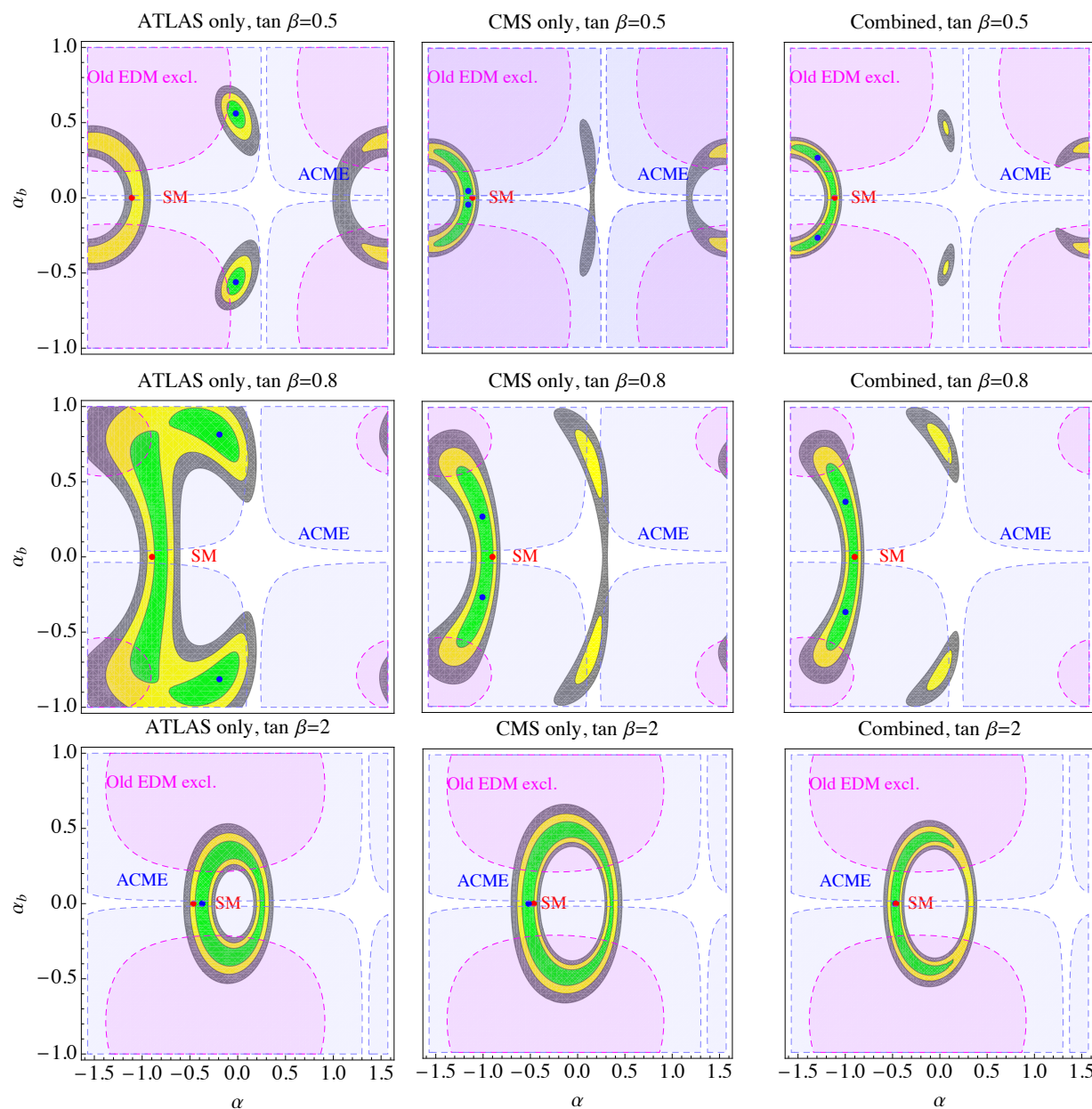
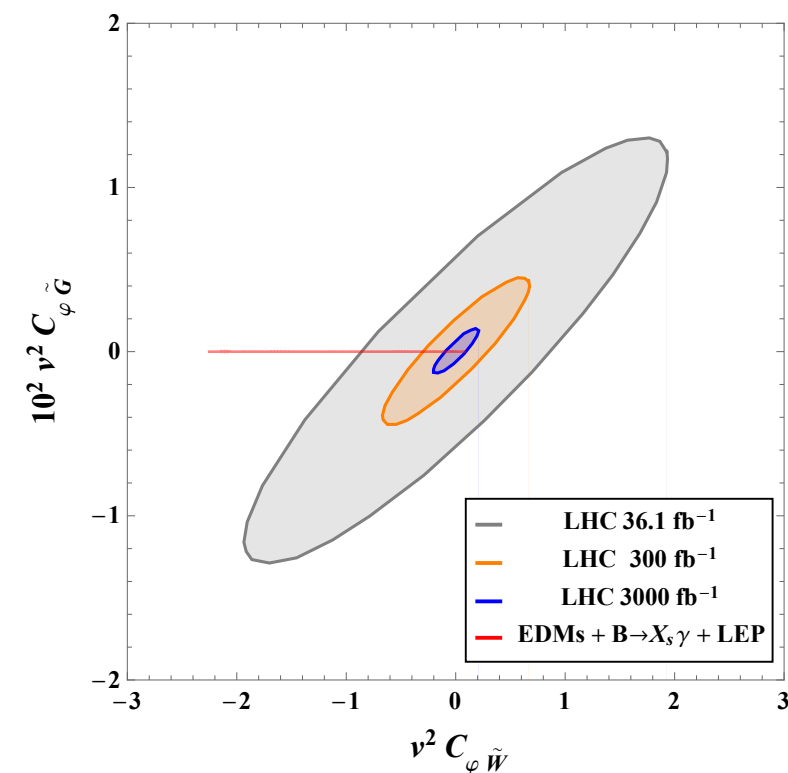
- motivated $f_{CP} < 0.01$ ($\alpha_b < 0.1$)
- to be updated to more recent results

• EFT analysis of EDM and LHC:

From tabletop to the LHC: [arXiv:1903.03625](https://arxiv.org/abs/1903.03625)



	Low energy	LHC (3000 fb ⁻¹)
$v^2 C_{\varphi\tilde{B}}$	$[-0.4, 0.00]$	$[-0.3, 0.3]$
$v^2 C_{\varphi\tilde{W}}$	$[-2.3, 0.02]$	$[-0.17, 0.17]$
$v^2 C_{\varphi\tilde{W}B}$	$[-1.3, 0.01]$	$[-0.39, 0.39]$
$v^2 C_{\varphi\tilde{G}}$	$[-1.3, 1.3] \cdot 10^{-5}$	$[-9.0, 9.0] \cdot 10^{-4}$



Unique features of Facilities: $\gamma\gamma$ production

- Photon collider is unique with focus on $H\gamma\gamma$ coupling

- photon beam polarization is critical for CP
- most interesting parameter:

$$\mathcal{A}_3 = \frac{|A_{||}|^2 - |A_{\perp}|^2}{|A_{||}|^2 + |A_{\perp}|^2} = \frac{2\mathcal{R}e(A_{--}^* A_{++})}{|A_{++}|^2 + |A_{--}|^2} = \frac{|a_2|^2 - |a_3|^2}{|a_2|^2 + |a_3|^2} = (1 - 2f_{CP})$$

Detecting and Studying Higgs Bosons at a Photon-Photon Collider: [arXiv:hep-ph/0110320](https://arxiv.org/abs/hep-ph/0110320)

- measure as asymmetry between $||$ and \perp linear polarizations

for $E_0 = 110$ GeV and $\lambda = 1 \mu\text{m}$: $f_{CP} = \sin^2(\alpha^{\gamma\gamma}) \sim \pm 0.06$

at $2.5 \cdot 10^{34} \times 10^7 = 250 \text{ fb}^{-1}$

- Interesting to revisit and compare to pp and e^+e^-

- need fair comparison: information from polarization, not cross section

Unique features of Facilities: $\mu^+\mu^-$ production

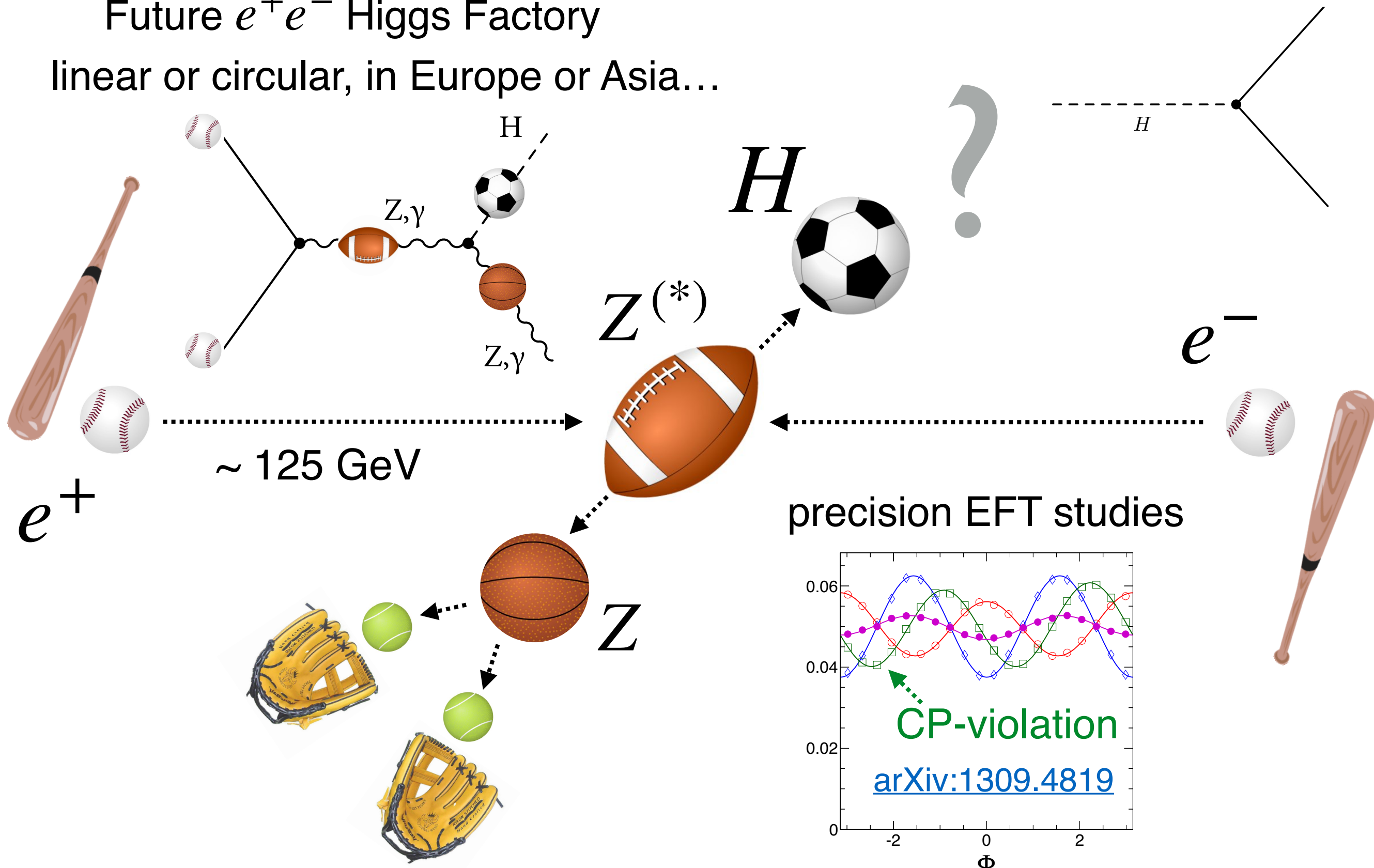
- Muon collider is unique with focus on $H\mu\mu$ coupling
 - muon beam transverse polarization is critical for CP
 - not many fermion couplings can be tested with polarization and CP
 - later we will discuss $H\tau\tau$ and Htt (both 3rd family)
 - same transverse polarization \Rightarrow CP-even
 - opposite polarization \Rightarrow CP-odd

How Valuable is Polarization at a Muon Collider? A Test Case: Determining the CP Nature of a Higgs Boson:
[arXiv:hep-ph/0003091](https://arxiv.org/abs/hep-ph/0003091)

- Unique feature of the muon collider
 - though comes with a price of lumi, likely not a priority at first stage

Unique features of Facilities: e^+e^- production

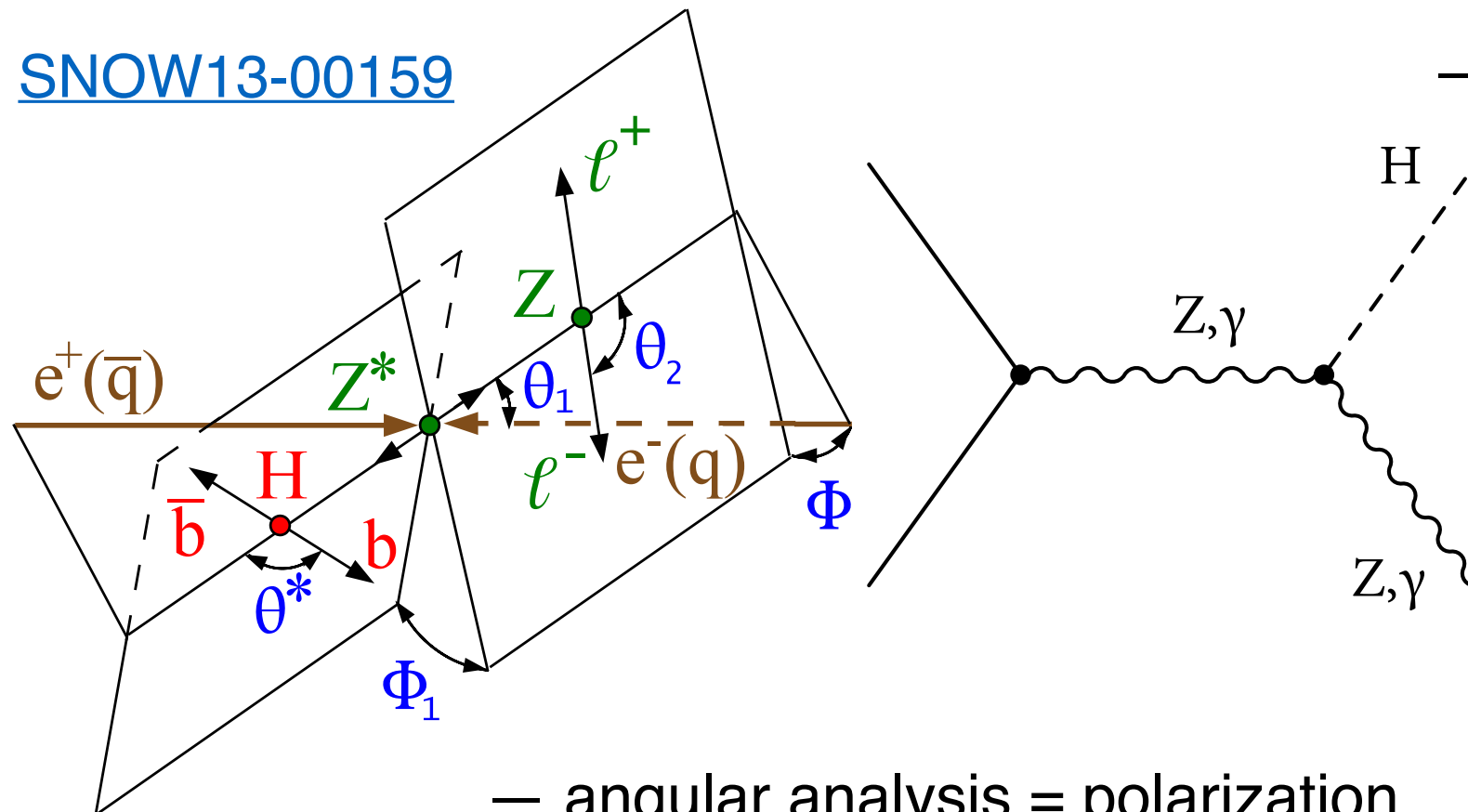
Future e^+e^- Higgs Factory
linear or circular, in Europe or Asia...



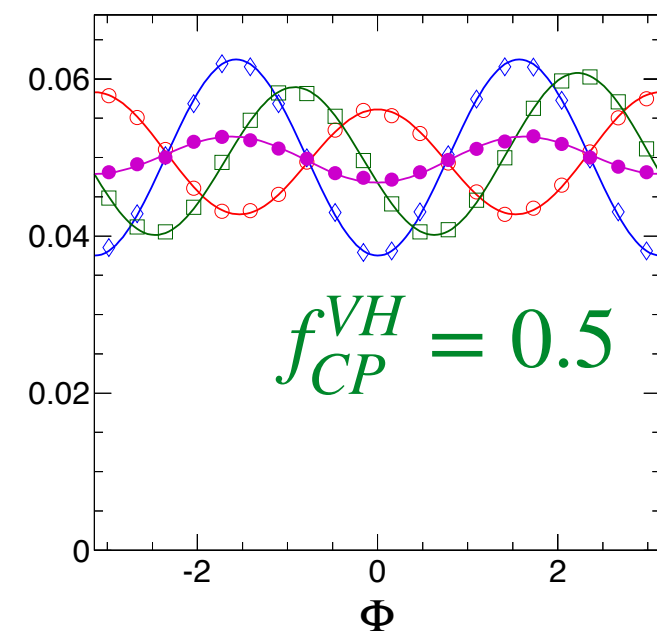
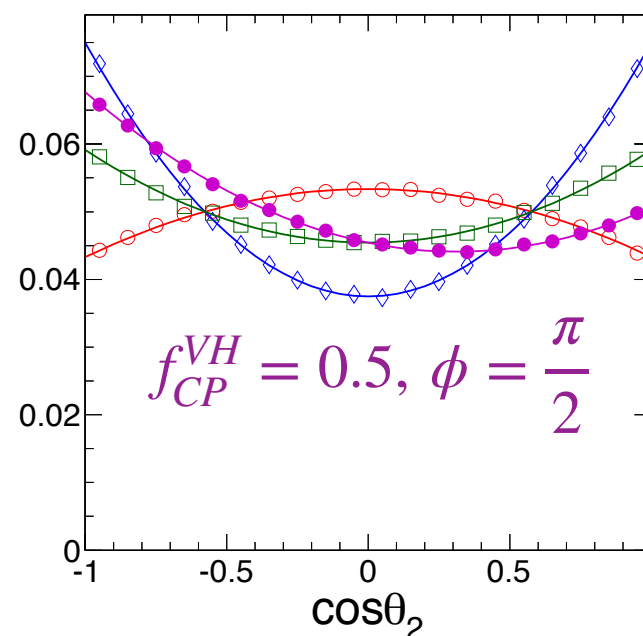
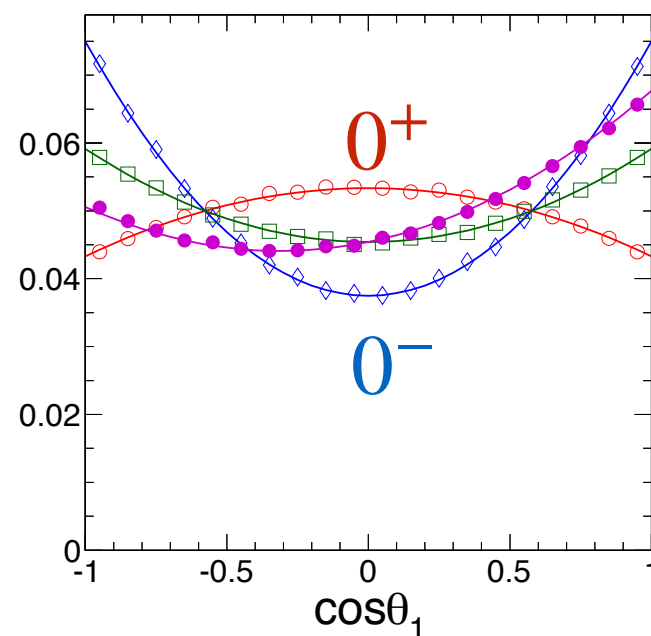
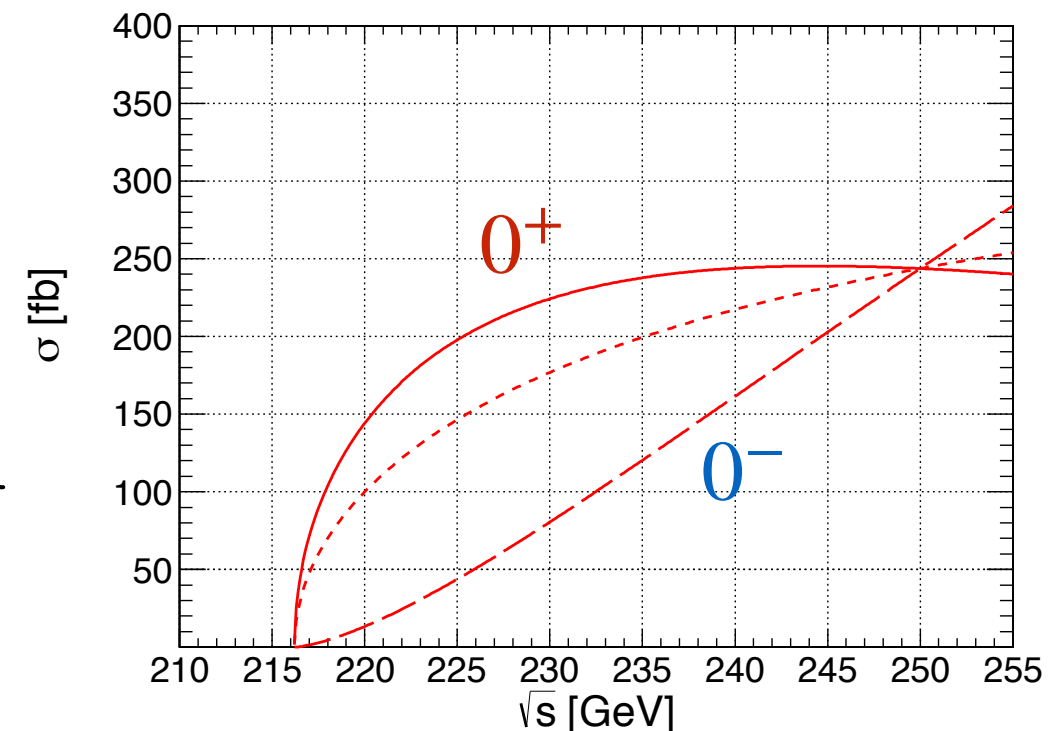
Unique features of Facilities: e^+e^- production

- e^+e^- collider $\rightarrow Z^* \rightarrow ZH \Rightarrow HZZ, HZ\gamma, H\gamma\gamma$ couplings

[SNOW13-00159](#)

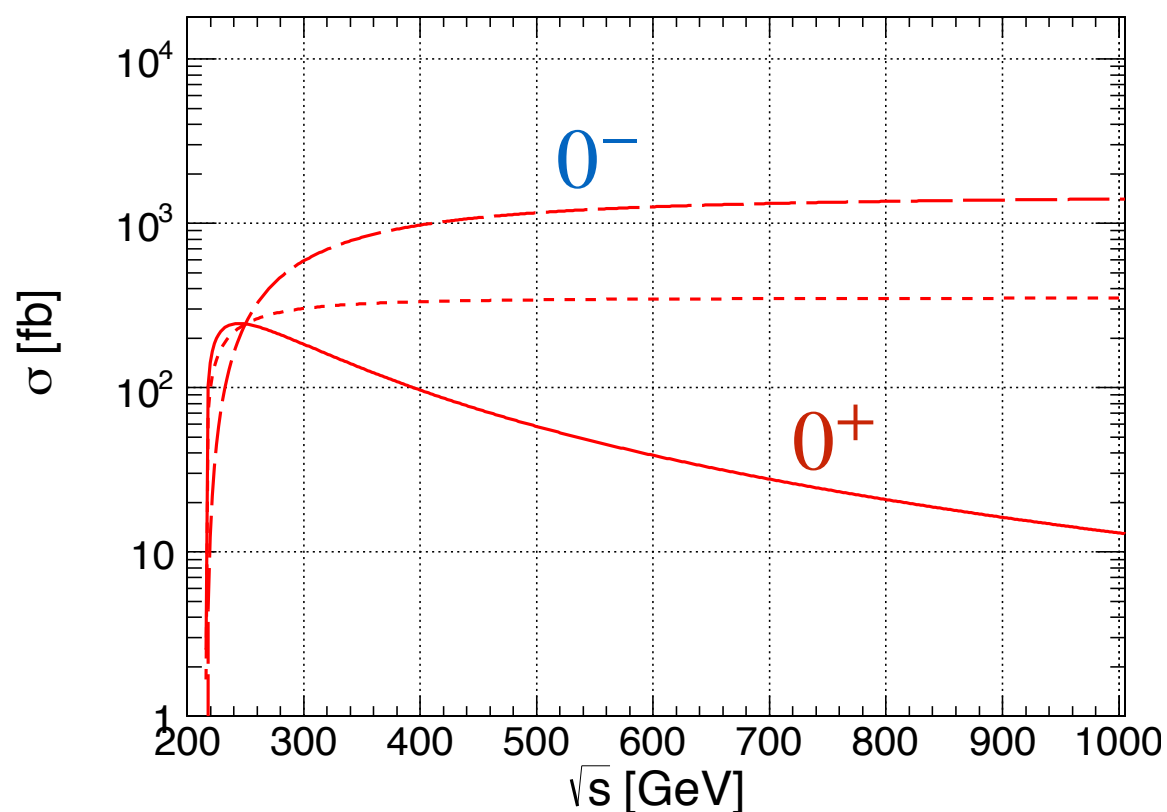


— threshold scan = q^2 dependence



e^+e^- production at higher energies (LC)

- e^+e^- collider $\rightarrow Z^* \rightarrow ZH$
- Scan q^2 dependence of HVV couplings
 \Rightarrow increased sensitivity (without cutoff)



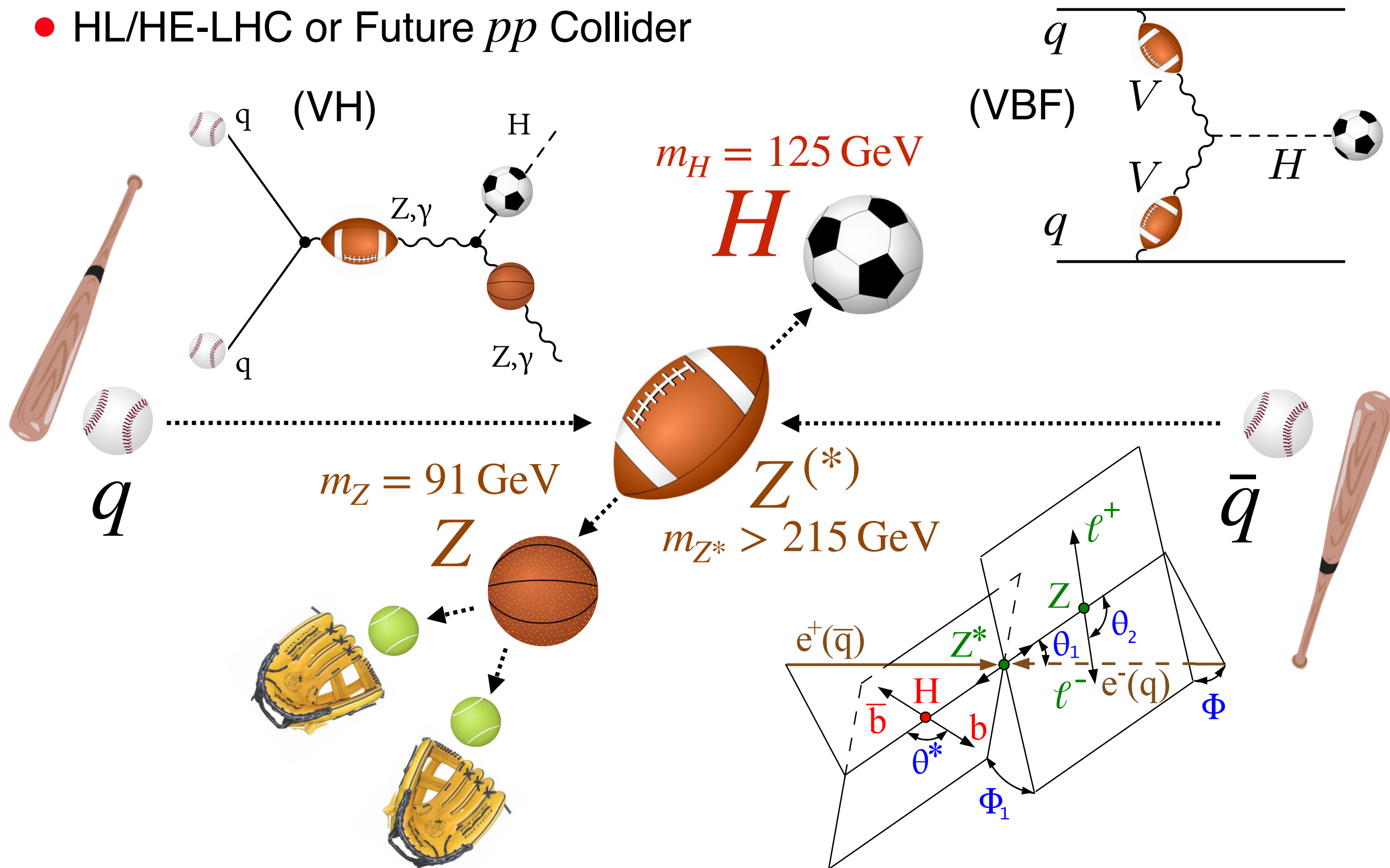
[SNOW13-00159](#)

- Linear collider $e^+e^- \rightarrow t\bar{t}H$
cross section dependence studied
of 0^+ vs. 0^-
need dedicated CP-sensitive study
(see LHC studies)

- VBF $e^+e^- \rightarrow \nu\bar{\nu}H$
not much angular information
 q^2 -dependence through $p_T^H \dots$

Unique features of Facilities: pp production

- HL/HE-LHC or Future pp Collider



Unique features of Facilities: pp production

- $pp \rightarrow V^* \rightarrow VH \Rightarrow HWW, HZZ, HZ\gamma, H\gamma\gamma, Hgg$ couplings

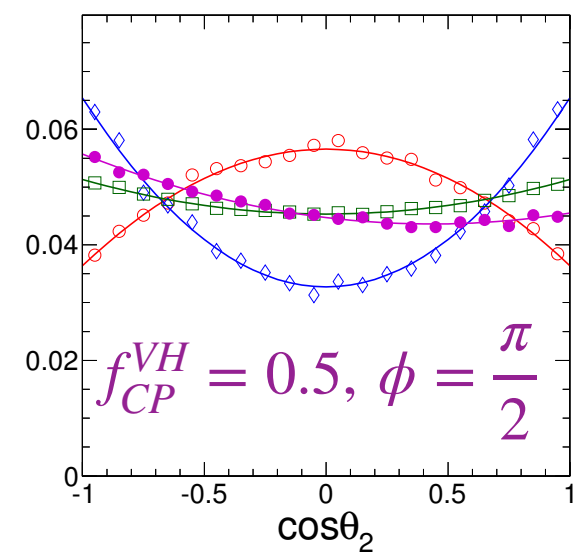
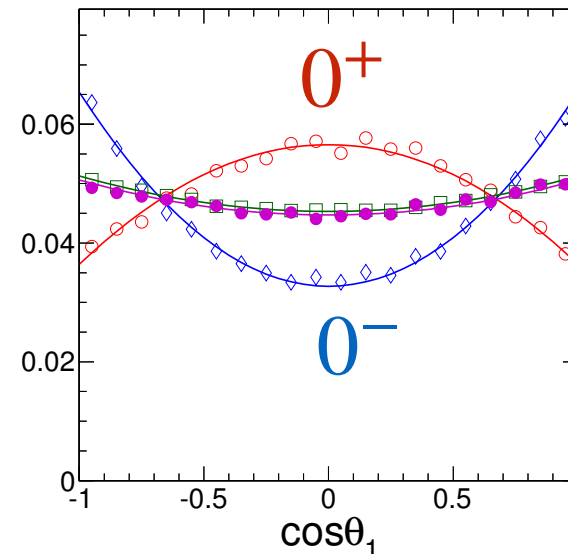
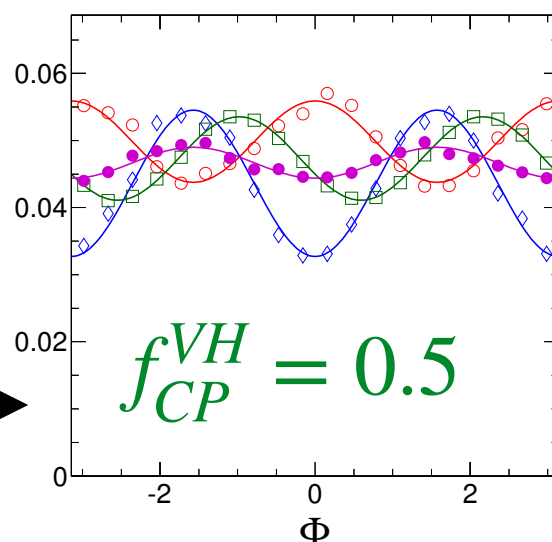
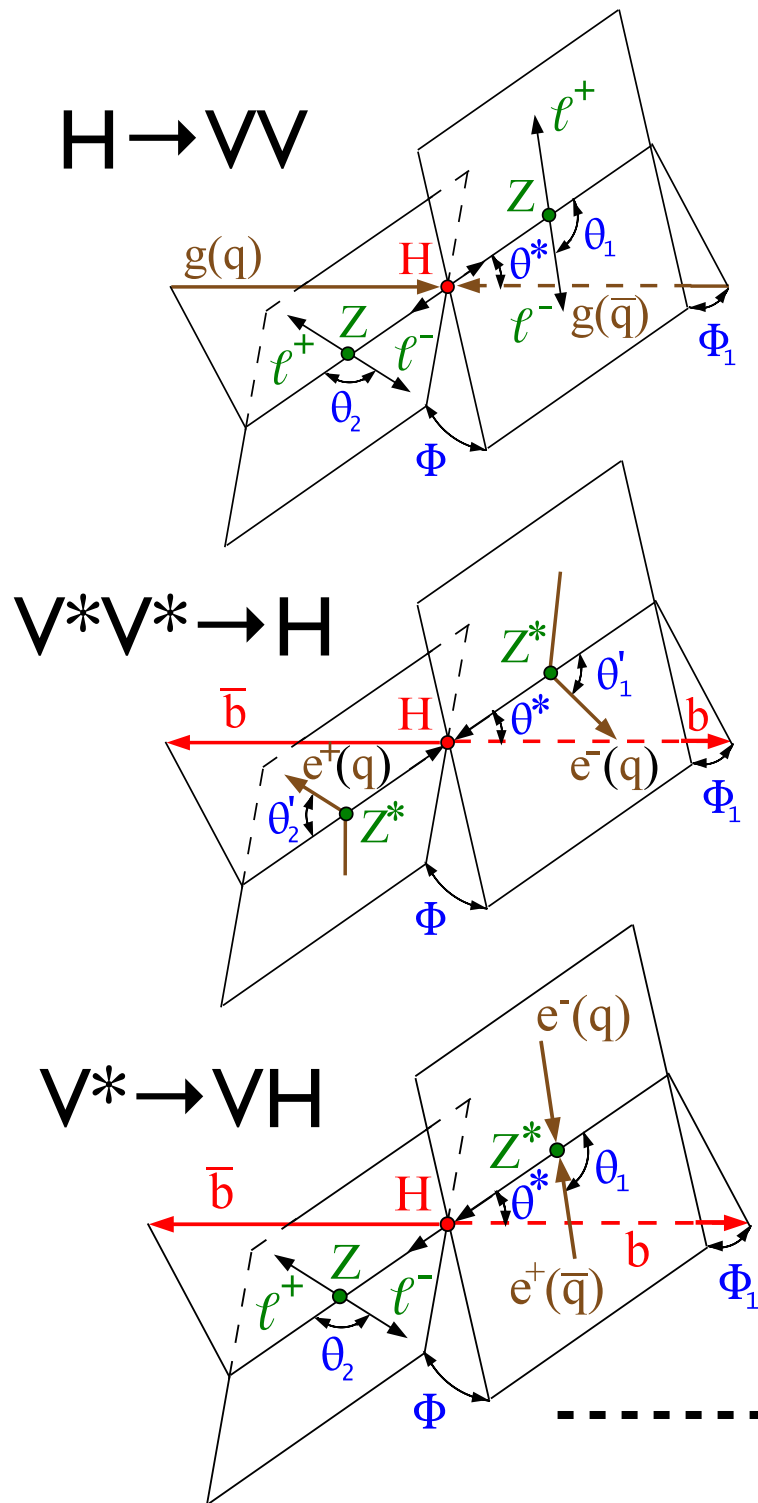
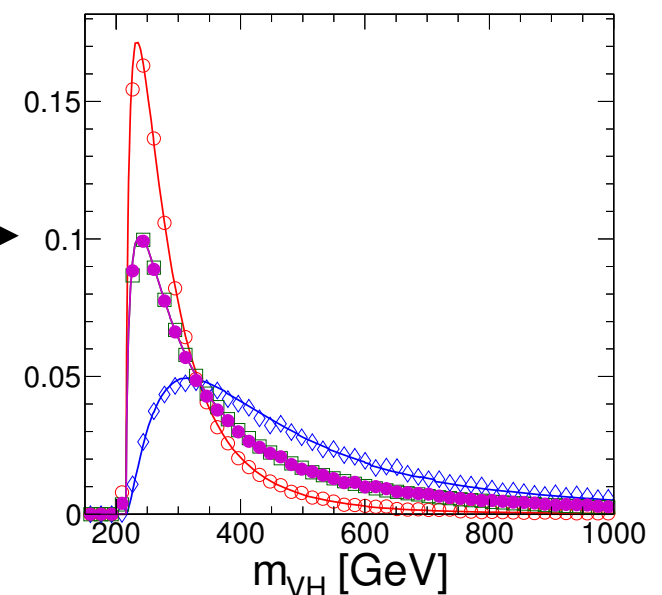
also VBF $V^*V^* \rightarrow H$ and decay $H \rightarrow VV$

pp unique $gg \rightarrow H$

benefit from LHC experience

- scan of q^2 -dependence
- polarization measurement

[SNOW13-00159](#)

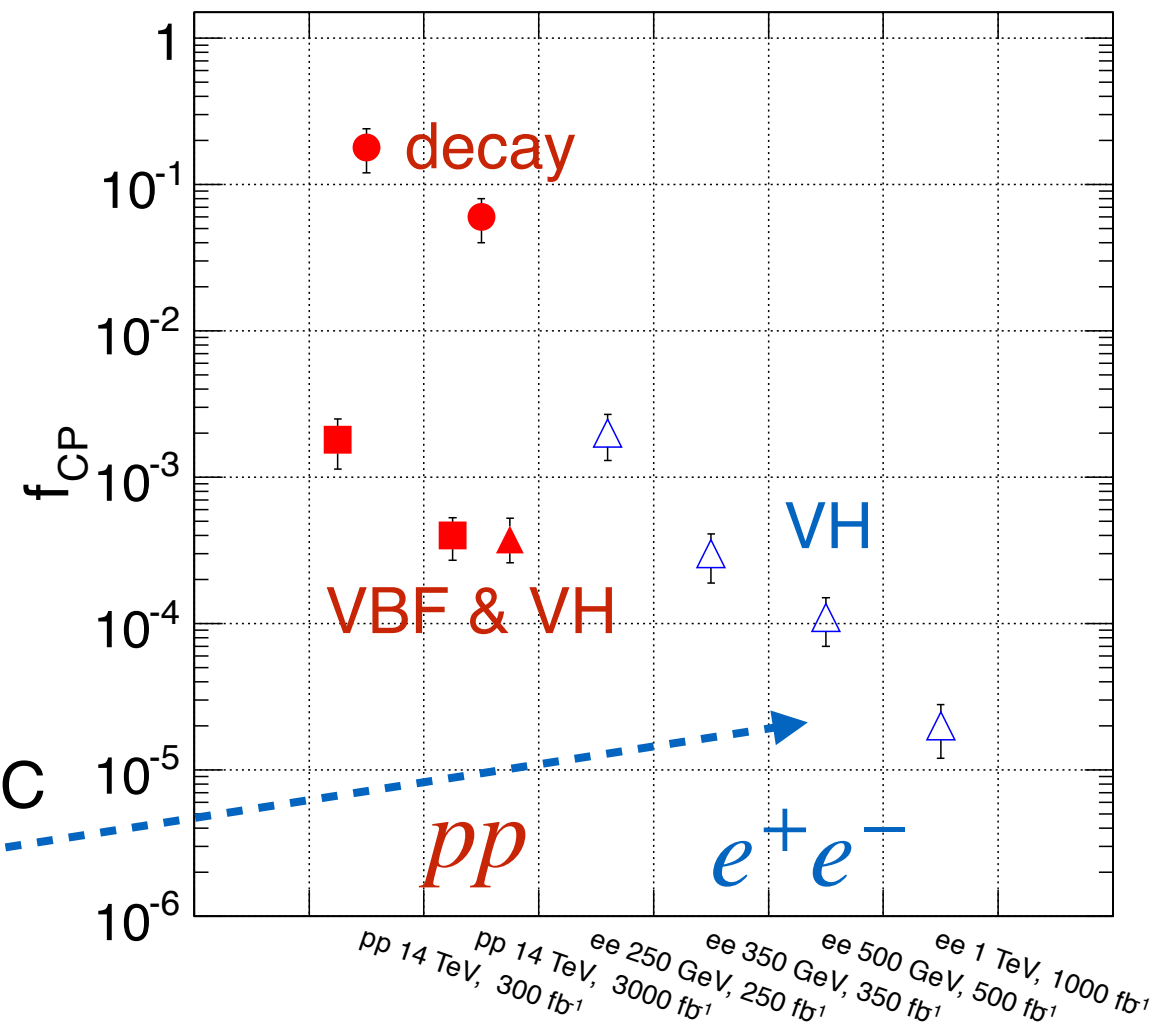


Compare Facilities: e^+e^- and pp

- pp leads to wider spectrum of production modes, more decays
 - but reach in HVV comparable
 - $q^2 = s$ at e^+e^- , from PDFs at $pp \Rightarrow$ pros and cons

Collider	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-
E (GeV)	14,000	14,000	250	350	500	1,000
\mathcal{L} (fb^{-1})	300	3,000	250	350	500	1,000
VVH^\dagger	0.07	0.02	✓	✓	✓	✓
VVH^\ddagger	$4 \cdot 10^{-4}$	$1.2 \cdot 10^{-4}$	$7 \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$4 \cdot 10^{-5}$	$8 \cdot 10^{-6}$
VVH^\diamond	$7 \cdot 10^{-4}$	$1.3 \cdot 10^{-4}$	✓	✓	✓	✓
ggH	0.50	0.16	—	—	—	—

[arXiv:1310.8361](https://arxiv.org/abs/1310.8361)



- benefit from q^2 sensitivity at LC
- may want to compare with q^2 “roll-off” not clearly defined...

[SNOW13-00159](#)

Update to recent LHC projections to HL-LHC

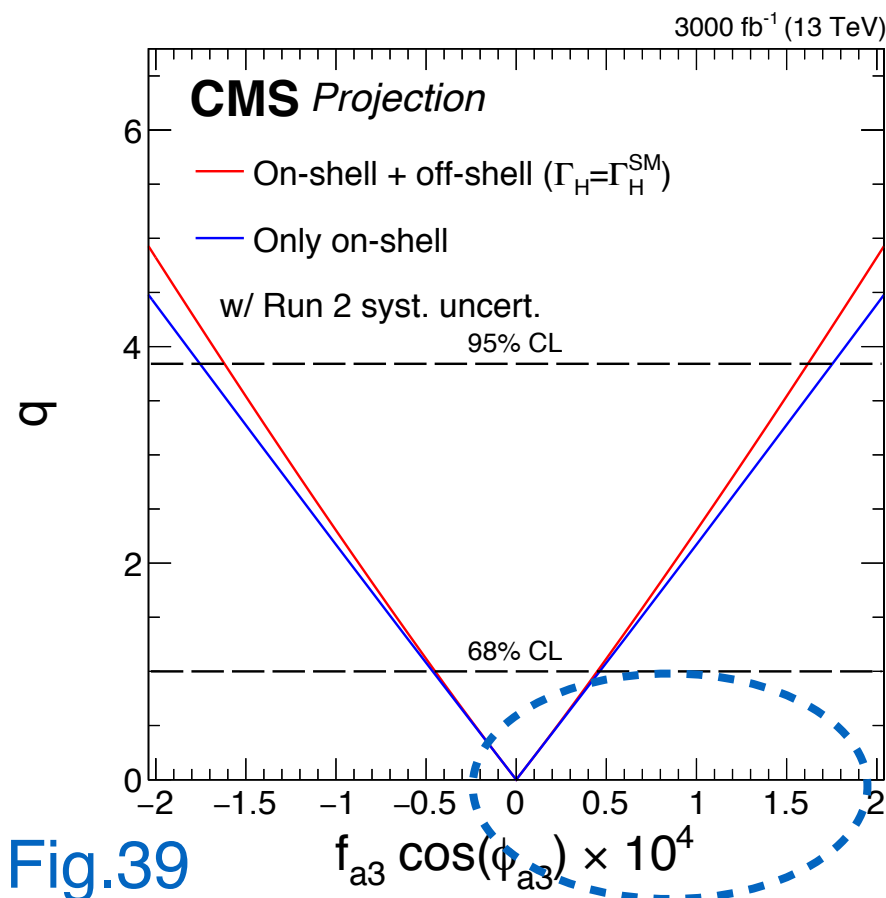
- Higgs Physics at the HL-LHC and HE-LHC

WG2 report: [arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

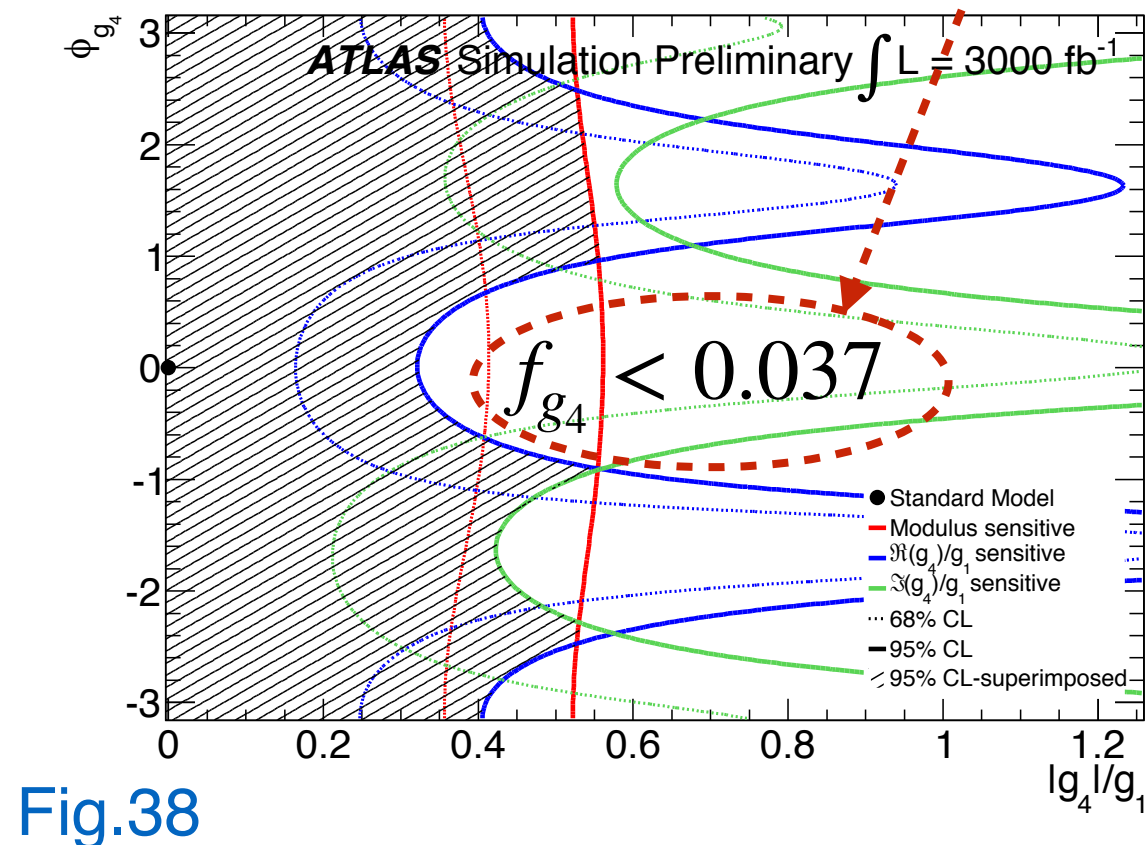
earlier HVV projections are confirmed:
with CMS & ATLAS full simulation

Collider	pp	pp
E (GeV)	14,000	14,000
\mathcal{L} (fb $^{-1}$)	300	3,000
VVH^\dagger	0.07	0.02
VVH^\ddagger	$4 \cdot 10^{-4}$	$1.2 \cdot 10^{-4}$
VVH^\diamond	$7 \cdot 10^{-4}$	$1.3 \cdot 10^{-4}$

$VV \rightarrow H \rightarrow 4\ell$ production



$H \rightarrow ZZ \rightarrow 4\ell$ decay



- agreement with most recent pheno HVV and Hgg projections [arXiv:2002.09888](https://arxiv.org/abs/2002.09888)

Update to recent LHC projections to HL-LHC

- Higgs Physics at the HL-LHC and HE-LHC

WG2 report: [arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

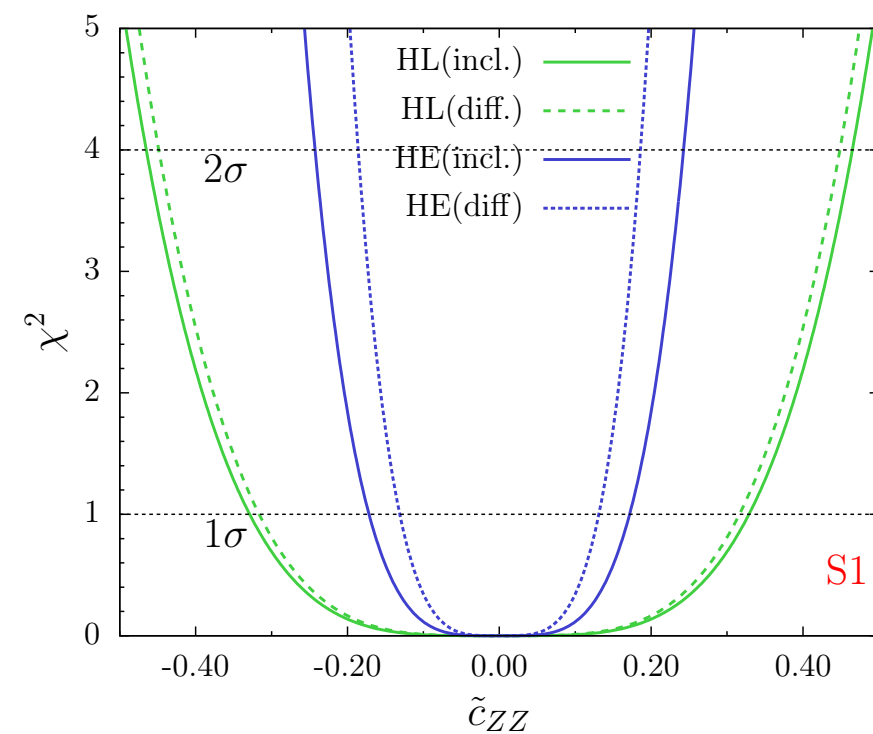
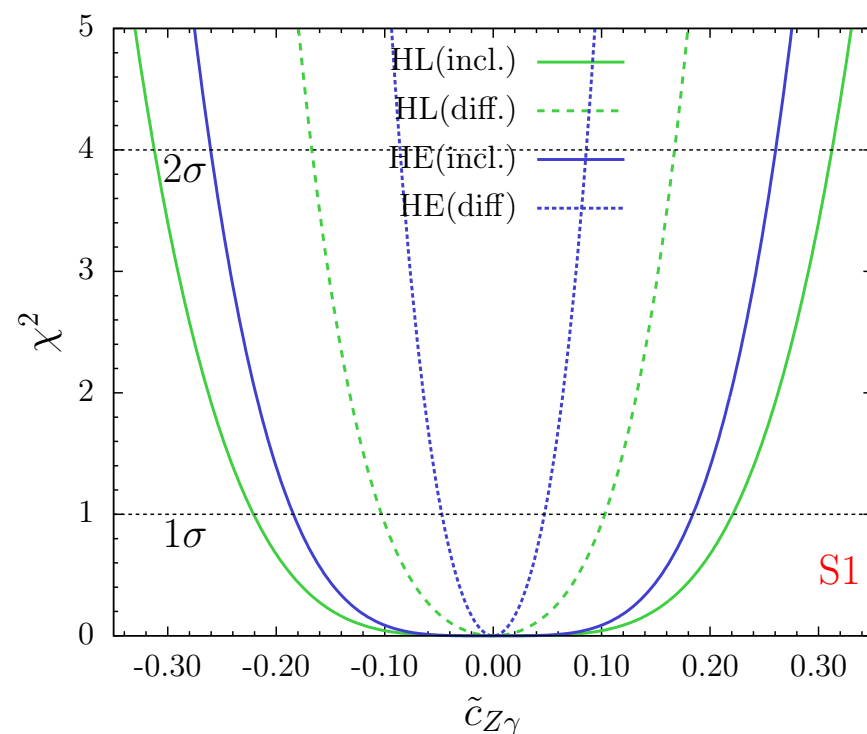
— Global fits also target CP-odd couplings

— be careful to interpret yield as CP...

$$\chi^2(\tilde{c}_{Z\gamma}, \tilde{c}_{ZZ}) = \sum_{i,f} \frac{(\mu_{i,f} - \mu_{i,f}^{\text{obs.}})^2}{\Delta_{i,f}^2}$$

CP-even CP-odd

$$\begin{aligned} \mu_{ZH}^{14\text{TeV}} &= 1.00 + 0.54 \tilde{c}_{Z\gamma}^2 + 2.80 \tilde{c}_{ZZ}^2 + 0.95 \tilde{c}_{Z\gamma} \tilde{c}_{ZZ} \\ \mu_{WH}^{14\text{TeV}} &= 1.00 + 0.84 \tilde{c}_{Z\gamma}^2 + 3.87 \tilde{c}_{ZZ}^2 + 3.63 \tilde{c}_{Z\gamma} \tilde{c}_{ZZ} \\ \mu_{\text{VBF}}^{14\text{TeV}} &= 1.00 + 0.25 \tilde{c}_{Z\gamma}^2 + 0.45 \tilde{c}_{ZZ}^2 + 0.45 \tilde{c}_{Z\gamma} \tilde{c}_{ZZ} \end{aligned}$$



Fermion couplings: $t\bar{t}H$ at pp

- Very first test of CP in Hff last year:

- $t\bar{t}H$ spin-off from Snowmass-2013

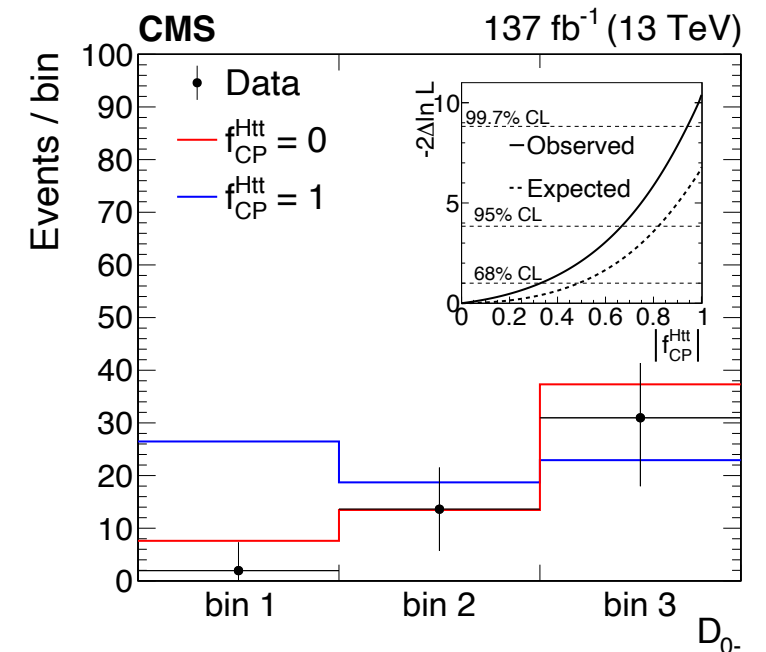
pheno projection agreement with CMS/ATLAS: [arXiv:1606.03107](https://arxiv.org/abs/1606.03107)

- reach $f_{CP} \sim 0.1$ ($\alpha \sim 18^\circ$) at HL-LHC

- no sensitivity to $2\text{Re}\left(A_{CP\text{even}}A_{CP\text{odd}}^*\right)$

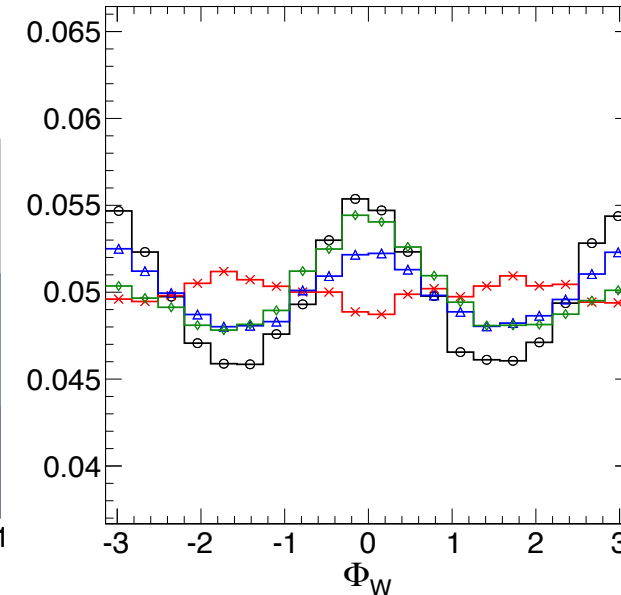
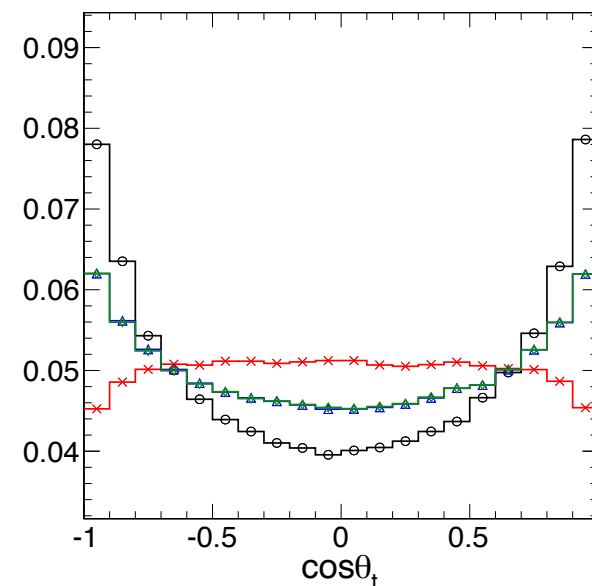
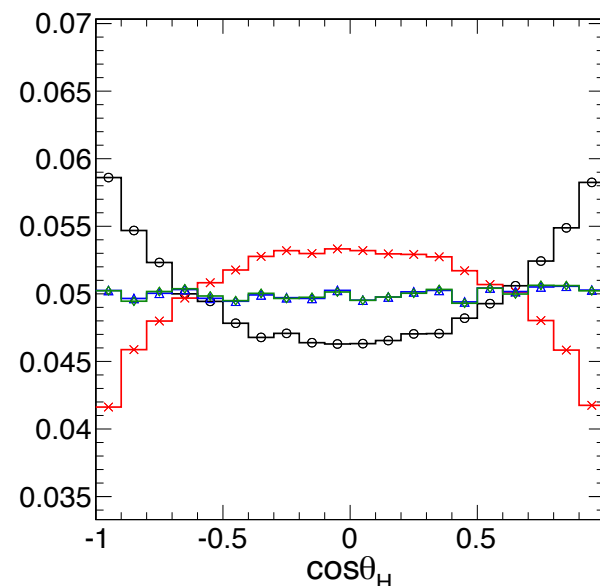
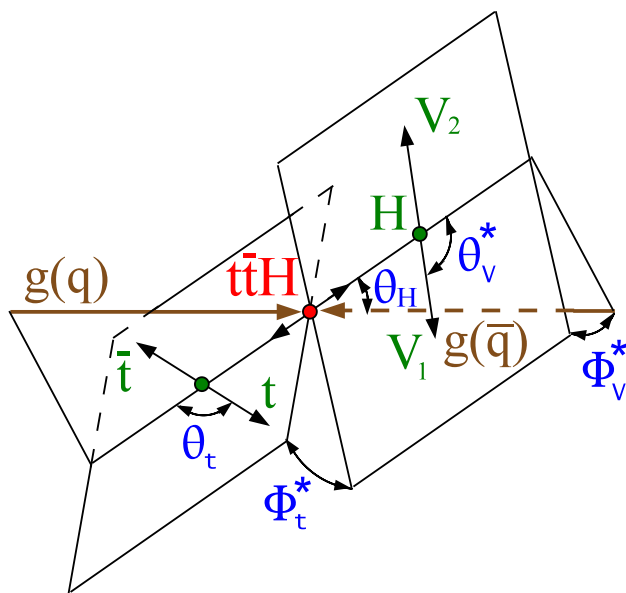
- need di-lepton channel for CP interf: [arXiv:1507.07926](https://arxiv.org/abs/1507.07926)

- similar in tH ; no sensitivity to $b\bar{b}H$, or other light q



CMS [arXiv:2003.10866](https://arxiv.org/abs/2003.10866)

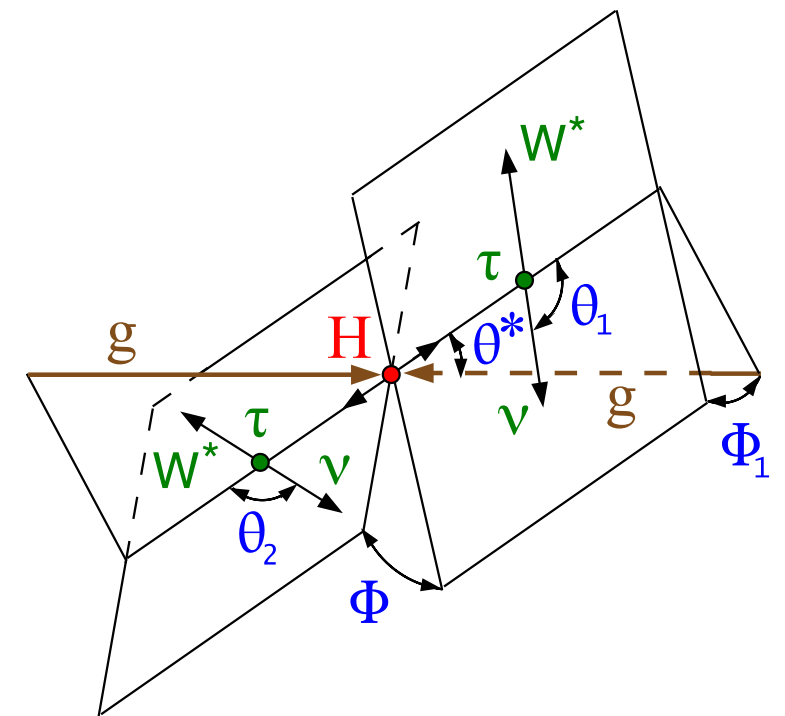
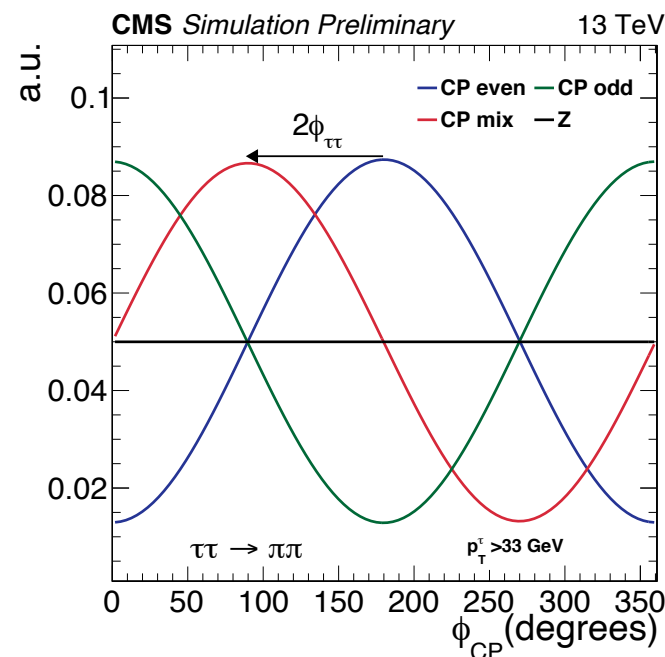
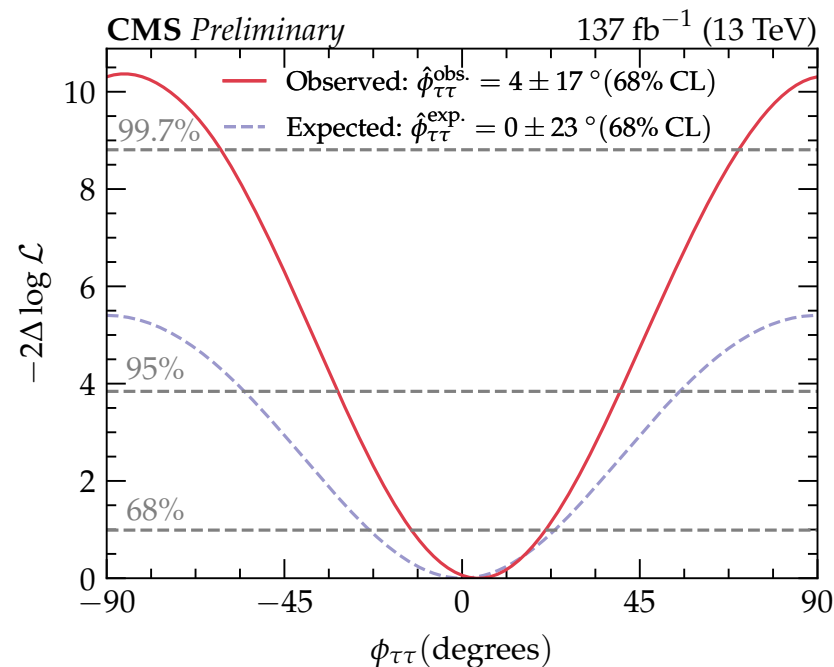
ATLAS [arXiv:2004.04545](https://arxiv.org/abs/2004.04545)



- Make comparison to LC e^+e^- , but looks statistics limited...

Decay: $H \rightarrow \tau^+ \tau^-$ at pp

- Very first test of CP in $H\tau\tau$ last year: CMS: [CMS-HIG-20-006](#)



pp pheno studies at Snowmass-2013: [arXiv:1308.1094](#)

- reach $f_{CP} \sim 0.04$ ($\alpha \sim 11^\circ$) at HL-LHC
- will benefit from CMS (above) and ATLAS (?) studies, may be $\alpha \sim 5^\circ$?

e^+e^- pheno studies at Snowmass-2013: [arXiv:1308.2674](#)

- the only CP in Hff at e^+e^- $\sqrt{s} < 500 \text{ GeV}$
- reach $f_{CP} \sim 0.008$ ($\alpha \sim 5^\circ$) at e^+e^- ref. lumi

Summary and Plans

- Higgs CP is a good **reference measurement** for **Snowmass-2022**
 - **Snowmass-2013** is already a good starting point
 - Gitlab area created: <https://gitlab.cern.ch/snowmass21-ef01/higgs-cp>

- Benefit from the past 8 years + 1 year ahead

- sharpen **theoretical** expectations / models
- connect to broader **EFT**
- recent ATLAS & CMS analyses provide good guide for **pp**
- comparison to **e^+e^-** may be improved
- **$\gamma\gamma$** & **$\mu^+\mu^-$** date back to **Snowmass-2001**, but may be not a priority...

$$f_{\text{CP}}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$

- Focus on CP in:
 - HWW, HZZ** – dominant tree-level **HVV**
 - $HZ\gamma, H\gamma\gamma, Hgg$** – loop **$HVV$** with massless **$V$**
 - $Htt, H\tau\tau, H\mu\mu$** – fermion **Hff**

& think about anything else...

BACKUP

Targeted CP-sensitive Couplings

- Look at effective couplings, either within EFT or not

$$f_{\text{CP}}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$

(same for $H \rightarrow \gamma\gamma, Z\gamma$)

CP-even a_2^{gg} & CP-odd a_3^{gg} couplings

e.g. fermion loop $a_2^{gg} = -\alpha_s \kappa_Q / (6\pi)$ & $a_3^{gg} = -\alpha_s \tilde{\kappa}_Q / (4\pi)$

- Target HVV, Hgg, Hff couplings

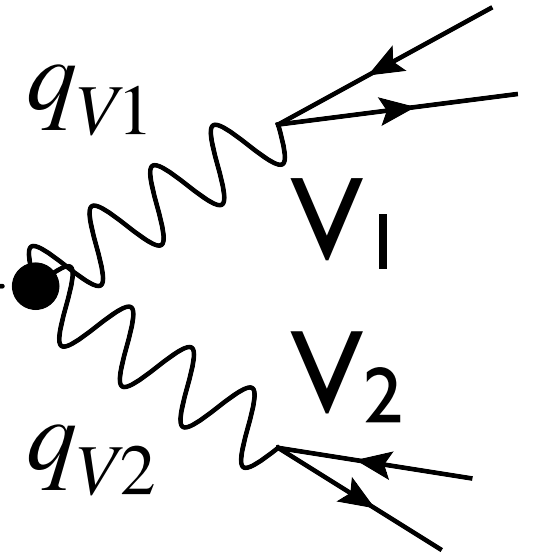
$$A(Hff) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i \tilde{\kappa}_f \gamma_5) \psi_f$$

CP-even CP-odd

Targeted CP-sensitive Parameters

- Somewhat more complicated with $V=Z,W$

$$A(HVV) = \frac{1}{v} \left[\underbrace{a_1^{VV}}_{\text{tree-level SM}} + \frac{\kappa_1^{VV} q_{V1}^2 + \kappa_2^{VV} q_{V2}^2}{(\Lambda_1^{VV})^2} + \frac{\kappa_3^{VV} (q_{V1} + q_{V2})^2}{(\Lambda_Q^{VV})^2} \right] m_{V1}^2 \epsilon_{V1}^* \epsilon_{V2}^* - \frac{H}{- - -} - \bullet \left[\underbrace{\frac{1}{v} a_2^{VV} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu}}_{\text{CP-even}} + \underbrace{\frac{1}{v} a_3^{VV} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}}_{\text{CP-odd}} \right]$$



- May attempt full EFT expansion, but not necessarily the goal in this study...

$$\left| A_{\text{CP even}} \right|^2 + 2\text{Re} \left(A_{\text{CP even}} A_{\text{CP odd}}^* \right) + \left| A_{\text{CP odd}} \right|^2$$

do not constrain
to SM rate

$$\int = 0 \Rightarrow \text{kinematic distributions}$$

true CP-sensitive observation
but not always available

suppressed in EFT

have to be clear if
this term dominates

$$f_{CP} = \frac{\left| A_{\text{CP odd}} \right|^2}{\left| A_{\text{CP even}} \right|^2 + \left| A_{\text{CP odd}} \right|^2} = \sin^2(\alpha_{\text{eff}})$$

parameter of interest

$$f_{CP}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{\text{CP odd}}}{\Gamma_{H \rightarrow X}^{\text{CP odd}} + \Gamma_{H \rightarrow X}^{\text{CP even}}}$$